$\qquad$

## Estimation and Number Theory

## Worksheet 1 Estimation

Find each sum or difference. Then use rounding to check that your answer is reasonable. Round each number to the nearest 100.

Example

| $475+382=?$ |
| :--- |
| $475+382=$857  <br> Number Rounded to the nearest 100 <br> 475 500 <br> 382 400 <br> answer is reason  |
| Add |

The estimated sum is $\qquad$ 900


Is your answer reasonable? $\qquad$ Yes

1. Find $534+208$.
$534+208=$ $\qquad$

| Number | Rounded to the nearest 100 |
| :---: | :---: |
| 534 |  |
| 208 |  |
| Add |  |

The estimated sum is $\qquad$
Is your answer reasonable? $\qquad$
2. Find $836-487$.
$836-487=$ $\qquad$

| Number | Rounded to the nearest 100 |
| :---: | :---: |
| 836 |  |
| 487 |  |
| Subtract |  |

The estimated difference is $\qquad$
Is your answer reasonable? $\qquad$
$\qquad$
$\qquad$

Find each sum or difference. Then use rounding to check that your answer is reasonable. Round each number to the nearest 1,000 .

Example

$$
\begin{aligned}
& 1,398+4,687=? \\
& 1,398+4,687=6,085
\end{aligned}
$$ 6,085 is close to 6,000 , so the answer is reasonable.

| Number | Rounded to the nearest 1,000 |
| :---: | :---: |
| 1,398 | 1,000 |
| 4,687 | 5,000 |
| Add | 6,000 |

Is your answer reasonable? $\qquad$ Yes
3. Find $4,772+2,409$.
$4,772+2,409=$ $\qquad$

| Number | Rounded to the nearest 1,000 |
| :---: | :--- |
| 4,772 |  |
| 2,409 |  |
| Add |  |

Is your answer reasonable? $\qquad$
4. Find $14,842-9,221$.
$14,842-9,221=$ $\qquad$

| Number | Rounded to the nearest 1,000 |
| :---: | :--- |
| 14,842 |  |
| 9,221 |  |
| Subtract |  |

Is your answer reasonable?

## Estimate each sum or difference using front-end estimation.

Example

$$
7,389-2,543=?
$$

The leading digit

$$
\text { (7, } 389-2,54
$$ of 7,389 is 7 .

$$
\underline{7,000}-\underline{2,000}=\underline{5,000}
$$

The leading digit of 2,543 is 2 .
5. $3,351+1,469$
6. $9,217-2,881$

Name: $\qquad$ Date: $\qquad$

Find each sum or difference. Then use front-end estimation to check that your answer is reasonable.

Example

$$
478+403=881
$$



Estimated sum: $\quad 400$ _ $+\underline{400}=\underline{800}$

Explain: 881 is close to 800 , so the answer is reasonable.
7. $798-465=$ $\qquad$


Estimated difference: $\qquad$ - $\qquad$ $=$

Explain: $\qquad$
8. $2,326+3,639=$ $\qquad$

$$
\underset{\downarrow}{\text { (2),326 }}+\underset{\downarrow}{\text { 3, }} \mathbf{\downarrow}
$$

Estimated sum: $\qquad$ $+$ $\qquad$
$\qquad$

Explain: $\qquad$
9. $5,389-2,658=$ $\qquad$


Estimated difference: $\qquad$ - $\qquad$ $=$ $\qquad$

Explain:
$\qquad$

Find each product. Then use rounding to check that your answer is reasonable.

Example


Is the answer reasonable? $\qquad$ Yes

10. $326 \times 3=$ $\qquad$
$\square$
Is the answer reasonable? $\qquad$
11. $267 \times 2=$ $\qquad$

| Number | Rounded to the nearest <br> $100 \times 2$ |
| :---: | :---: |
|  |  |

Is the answer reasonable? $\qquad$

Name: $\qquad$ Date: $\qquad$

Find each product. Then use front-end estimation to check that your answer is reasonable.

Example
$79 \times 5=\underline{395}$
(7) $9 \times 5$
$70 \times 5=$ 350

The estimated product is $\qquad$ _.

Explain: $\frac{395 \text { is close to } 350 \text {, so the answer is reasonable. }}{\text { the }}$
12. $54 \times 4=$ $\qquad$

$$
(5) 4 \times 4
$$

Estimated product: $\qquad$ $\times 4=$ $\qquad$

Explain:
13. $112 \times 3=$ $\qquad$

$$
\text { (1) } 12 \times 3
$$

Estimated product: $\qquad$ $\times 3=$ $\qquad$

Explain:
$\qquad$

Find each quotient. Then use related multiplication facts to check that your answer is reasonable.

Example

| $741 \div 3$ | 24 |
| :---: | :---: |
|  | $3 \longdiv { 7 4 }$ |
| $741 \div 3=247$ | 600 |
|  | 14 |
| $3 \times 240=720$ | 120 |
|  | 21 |
| $3 \times 250=750$ | 21 |

Estimated quotient:

$$
750 \div 3=250
$$

The answer is reasonable.

741 is closer to 750 than 720 . So, $741 \div 3$ rounds to $750 \div 3$.
14. $496 \div 4=$ $\qquad$
$4 \times$ $\qquad$ $=$ $\qquad$
$4 \times$ $\qquad$ $=$ $\qquad$
Estimated quotient: $\qquad$ $\div 4=$ $\qquad$
The answer is $\qquad$
15. $516 \div 2=$ $\qquad$
$\underline{ }$ $\times$ $\qquad$ $=$
$\qquad$ $\times$ $\qquad$

$$
=
$$

$\qquad$

Estimated quotient: $\qquad$ $\div$ $\qquad$ $=$ $\qquad$
The answer is $\qquad$ _.

Name: $\qquad$
$\qquad$
16. $780 \div 5=$ $\qquad$
$\qquad$
$\qquad$
Estimated quotient: $\qquad$ $\div$ $\qquad$ = $\qquad$
The answer is $\qquad$ .

Solve. Decide whether to find an estimate or an exact answer.

## Example

724 meters of barbed wire is needed to enclose a park. How much barbed wire is needed to enclose 4 identical parks?
$724 \mathrm{~m} \times 4=2,896 \mathrm{~m}$

2,896 meters of barbed wire is needed.

An exact answer is needed because the question asks how much barbed wire is needed.

17. Ms. Katy has $\$ 111$. She wants to spend $\$ 52$ on books, $\$ 33$ on fruit, and $\$ 21$ on vegetables. Does she have enough money to buy all these things?
18. A bottle contains 784 milliliters of milk. A family drinks 309 milliliters of milk in the morning and the rest of the milk in the afternoon. How much milk do they drink in the afternoon?
19. Caithlin spent $\$ 14.99$ on a sweater, $\$ 5.29$ on 2 pairs of socks, and $\$ 8.99$ on a blouse. About how much money did Caithlin spend in all?
$\qquad$

## Worksheet 2 Factors

Write the missing numbers.
Example
$14 \times 3=$ $\qquad$

42 can be divided exactly by $\qquad$ and $\qquad$

1. $21 \times 5=$ $\qquad$
$\qquad$ can be divided exactly by 21 and $\qquad$
2. $35 \times 3=$ $\qquad$
$\qquad$ can be divided exactly by $\qquad$ and $\qquad$

## Write the missing numbers.

Example

$$
12 \times 3=\frac{36}{}
$$

36 is a product of 12 and 3.
12 and 3 are factors of $\qquad$ .

Whole numbers can be broken into factors.
3. $8 \times 12=$ $\qquad$
$\qquad$ is a product of 8 and 12 .
$\qquad$ and $\qquad$ are factors of $\qquad$
4. $26 \times 4=$ $\qquad$
$\qquad$ is a product of 26 and 4 .
$\qquad$ and $\qquad$ are factors of $\qquad$
$\qquad$

Find the quotient. Then write the missing words.

5. $14 \div 5=$ $\qquad$
Can 14 be divided exactly by 5 ? $\qquad$
Is 5 a factor of 14 ? $\qquad$
6. $18 \div 6=$ $\qquad$
Can 18 be divided exactly by 6 ? $\qquad$
Is 6 a factor of 18 ? $\qquad$
7. $28 \div 7=$ $\qquad$
Can 28 be divided exactly by 7 ? $\qquad$
Is 7 a factor of 28 ? $\qquad$
$\qquad$
$\qquad$

Find the factors of each number.
Example

$$
\begin{aligned}
8 & =1 \times 8 \\
& =2 \times 4
\end{aligned}
$$

The factors of 8 are $1,2,4$, and 8 .

A whole number can be written as a product of factors.
8. $24=1 \times 24$

$$
=2 \times
$$

$\qquad$
$=$ $\qquad$
$=$ $\qquad$ $\times 6$

The factors of 24 are $\qquad$ $\longrightarrow, ~-\quad$,
$\longrightarrow$, and $\qquad$
9. $54=$ $\qquad$ $\times$ $\qquad$

$$
\begin{aligned}
& =\square \times \square \\
& =\square \\
& =\square
\end{aligned}
$$

The factors of 54 are $\qquad$ — $\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$ and $\qquad$
10. $72=$ $\qquad$ $\times$

$$
\begin{aligned}
& =\_\times \\
& =\square
\end{aligned}
$$

$$
=\ldots
$$

$$
=\ldots
$$

$$
=
$$

$\qquad$ $\times$ $\qquad$
The factors of 72 are $\qquad$ ——

11. $108=$ $\qquad$ $\times$ $\qquad$

$$
=\ldots
$$

$$
=\ldots
$$

$\qquad$

$$
=\ldots
$$

$$
=\ldots \times
$$

$\qquad$

$$
=\ldots \times
$$

$\qquad$
The factors of 108 are $\qquad$
$\qquad$

$\qquad$
$\longrightarrow, \ldots, \ldots$, and $\quad, \quad$ _ $\quad$.
$\qquad$
$\qquad$

## Divide. Then answer each question.

Example
$15 \div 2=\frac{7 R 1}{8}$
$16 \div 2=\frac{8}{2}$ A common factor is a factor that is shared by two or more numbers.

Is 2 a common factor of 15 and 16 ? $\qquad$ No
12. $48 \div 3=$ $\qquad$
$52 \div 3=$ $\qquad$
Is 3 a common factor of 48 and 52? $\qquad$
13. $70 \div 5=$ $\qquad$
$95 \div 5=$ $\qquad$
Is 5 a common factor of 70 and 95 ? $\qquad$
14. $45 \div 8=$ $\qquad$
$96 \div 8=$ $\qquad$
Is 8 a common factor of 45 and 96 ? $\qquad$

## Find the factors of each pair of numbers. Then circle the common factors.

## Example

12 and 21

12: (1), 2, (3, $4,6,12$
21: (1), 3, 7, 21
Which of the circled common factors is the greatest?
15. 21 and 28

21: $\qquad$

28: $\qquad$
Which of the circled common factors is greatest? $\qquad$
16. 32 and 42

32: $\qquad$

42: $\qquad$
Which of the circled common factors is the greatest?
17. 48 and 72

48: $\qquad$

42: $\qquad$
Which of the circled common factors is the greatest? $\qquad$
$\qquad$

Find the greatest common factor of each pair of numbers.

## Example

16 and 24
Step 1 Divide 16 and 24 by a common factor.


$$
16 \div 2=8,24 \div 2=12
$$

Step 2 Divide until 16 and 24 cannot be divided by a common factor other than 1 .

| 2 | 16,24 |
| :--- | :---: |
| 2 | 8,12 |
| 2 | 4,6 |
|  | 2,3 |

$$
\begin{aligned}
& 2 \text { and } 3 \text { have no common factor } \\
& \text { other than } 1 \text {. }
\end{aligned}
$$

$$
10 \div 2=8,24 \div 2=12
$$



Step 3 Multiply the common factors.

$$
2 \times 2 \times 2=8
$$

The greatest common factor is 8 .

Name: $\qquad$
18. $\quad 12$ and 24


$$
\ldots \times \ldots \times \ldots
$$

The greatest common factor is $\qquad$ .
19. 36 and 42

$\qquad$
The greatest common factor is $\qquad$
21. $\quad 15$ and 42

Answer the questions using these numbers.


Example
Which of the numbers have 2 as a factor?
$10,24,36$, and 54
$\qquad$
22. Which of the numbers have 3 as a factor?
23. Which of the numbers have 5 as a factor?
24. Which of the numbers have 3 and 5 as factors?

Find the factors of each number. Then decide whether the number is a prime number.

Example

$$
17=1 \times 17
$$

The factors of 17 are 1 and 17 . So, 17 is a prime number.
25. 5
26. 9

A prime number has only 2 different factors, 1 and itself.
27. 11
28. 26

Find the factors of each number. Then decide whether the number is a composite number.

Example

$$
\begin{aligned}
6 & =1 \times 6 \\
& =2 \times 3
\end{aligned}
$$

The factors of 6 are $1,2,3$, and 6 . So, 6 is a composite number.

A composite number has more than 2 different factors.
29. 20
30. 13
31. 63
32. 41

Which numbers in Exercises $\mathbf{2 9}$ to $\mathbf{3 2}$ are prime numbers?
33. The prime numbers are $\qquad$ and $\qquad$
34. Why did you choose those two numbers? Explain your reasoning.
$\qquad$
$\qquad$

## Worksheet 3 Multiples

Find the first eight multiples of each number.

A multiple of a number is the number multiplied by any whole number.

Example

$$
\begin{array}{llll}
1 \times 4=4 & 2 \times 4=8 & 3 \times 4=12 & 4 \times 4=16 \\
5 \times 4=20 & 6 \times 4=24 & 7 \times 4=28 & 8 \times 4=32
\end{array}
$$

The first eight multiples of 4 are $\qquad$
$\qquad$ 12
$\qquad$ 20 24 $\qquad$ and $\qquad$ 32

1. 6
$1 \times 6=\square$
$2 \times 6=\square$
$3 \times 6=\square$
$4 \times 6=\square$
$5 \times 6=\square$
$6 \times 6=\square$
$7 \times 6=\square$
$8 \times 6=\square$

The first eight multiples of 6 are $\qquad$
2. 8
$1 \times 8=\square$
$2 \times 8=\square$
$3 \times 8=\square$
$4 \times 8=\square$
$5 \times 8=\square$
$6 \times 8=\square$
$7 \times 8=\square$
$8 \times 8=\square$

The first eight multiples of 8 are $\qquad$
$\qquad$

## Circle the numbers that are not multiples of the given number.

## Example

$$
4: \quad 4,14,16,20, \text { (34), } 44
$$

4 is a factor of all the multiples of 4 .
The numbers $4,16,20$, and 44 can be divided exactly by 4 . So, they are multiples of 4 .
3. $3: 12,15,18,21,23$
4. $5: 5,15,25,51,55$
5. 7: $7,17,21,27,35,42,56,63$
6. $\quad 9: 18,36,39,45,47,49,54,63,72,79$

## Check $(\mathcal{V})$ the correct box. Then write the missing numbers and words.

Example
Is 14 a multiple of 2 ?
$2 \longdiv { 1 4 }$
$\begin{array}{r}14 \\ \hline 0\end{array}$
Use division to determine whether a number is a multiple of another number.


No, 14 is not a multiple of 2 . It cannot be divided exactly by 2 .

## Name:

$\qquad$
7. Is 24 a multiple of 3 ?
Yes, 24 is the $\qquad$ multiple of 3 .
$\square$ No, 24 is not a multiple of 3 . It cannot be divided exactly by 3 .
8. Is 45 a multiple of 6 ?
Yes, 45 is the $\qquad$ multiple of 6 .
$\square$ No, 45 is not a multiple of 6. It cannot be divided exactly by 6 .
9. Is 96 a multiple of 8 ?Yes, 96 is the $\qquad$ multiple of 8 .No, 96 is not a multiple of 8 . It cannot be divided exactly by 8 .

## Circle the common multiples of each pair of numbers. Then write the missing numbers.

## Example

3:
$3,6,9,12,15,18,21,(24,27$
4: $4,8,(12), 16,20,(24,28,32,36$

A common multiple is a multiple that is shared between two or more numbers.

The common multiples are $\qquad$ and $\qquad$ 24

The least common multiple is the common multiple that is less than all the others.

The least common multiple is $\qquad$ .
10. $5: 5,10,15,20,25,30,35,40,45$

7: $7,14,21,28,35,42,49,56,63$
The common multiple is $\qquad$ .

The least common multiple is $\qquad$
11. $6: 6,12,18,24,30,36,42,48,54$

8: $8,16,24,32,40,48,56,64,72$
The common multiples are $\qquad$ and $\qquad$
The least common multiple is $\qquad$ .
$\qquad$
$\qquad$

Find the first two common multiples of each pair of numbers. Circle them and then write the least common multiple.

## Example

3 and 7
3: $3,6,9,12,15,18,(21), 24,27,30,33,36,39$, (42)
7: 7, 14, (21), 28, 35, (42, 49
The least common multiple is $\qquad$
12. 2 and 5

2: $\qquad$

5: $\qquad$
The least common multiple is $\qquad$
13. 6 and 9

6: $\qquad$

9: $\qquad$
The least common multiple is $\qquad$

Find the least common multiple of each pair of numbers using division.
Example
8 and 16
Step 1 Divide 8 and 16 until they cannot be divided by a common factor other than 1 .

$$
\begin{aligned}
& \text { There are } \\
& \text { five factors. } \\
& \text { Step } 2 \text { Multiply the factors. } \\
& 2 \times 2 \times 2 \times 1 \times 2=16 \\
& 2 \times 2 \times 16 \\
& 2
\end{aligned}
$$

16 is the least common multiple of 8 and 16 .
14. 9 and 18
15. 14 and 28
16. 15 and 45
17. 12 and 52
$\qquad$

## Worksheet 4 Multiplying Using Models

1. Study the array. Write a multiplication statement from the given diagram.
a.

b.

C.

2. Color dots to show the multiplication statement. Use white dots as 1 one. Cross out those unused dots.
a. $2 \times 15$

b. $\quad 4 \times 19$

3. Study the diagram. Then write a multiplication statement.
d.

$\qquad$
$=$
b.


$$
\begin{aligned}
9 \times \ldots & =\longleftarrow \times \\
& =\square
\end{aligned}
$$ $\times \ldots+$ $\qquad$ $\times$ $=$

4. Complete to show the multiplication.
a. $7 \times 14 \rightarrow 7 \times \ldots=$ So, $7 \times 14=\ldots+\ldots$
b. $\quad 5 \times 18 \rightarrow \longrightarrow \times 10=$ $\qquad$ $\times 8=$ $\qquad$
So, $5 \times 18=$ $\qquad$ $+$ $\qquad$ $=$ $\qquad$
c. $\quad 2 \times 16 \rightarrow 2 \times$ $\qquad$ $=$ $\qquad$
$\qquad$ $\times 6=$ $\qquad$
So, $2 \times 16=\ldots+$
d. $6 \times 15 \rightarrow$ $\qquad$ $\times 10=$ $\qquad$ $6 \times$ $\qquad$
$\qquad$ So, $6 \times 15=\ldots+\ldots$
$\qquad$
$\qquad$
5. Complete to show the multiplication.
a. $6 \times 13=$ $\qquad$ $\times$ $\qquad$ $+$ $\qquad$ $\times$ $\qquad$

$$
=
$$

$\qquad$

$$
+
$$

$\qquad$

$$
=
$$

$\qquad$
b. $4 \times 23=$ $\qquad$ $\times$ $\qquad$ $+\ldots$ $\qquad$

$$
=
$$

$\qquad$ $+$

$$
=
$$

$\qquad$
c. $5 \times 37=$ $\qquad$ $\times$ $\qquad$ $+$ $\qquad$ $\times$ $\qquad$

$$
=
$$

$\qquad$ $+$

$$
=
$$

$\qquad$
6. Multiply
a. $\quad 18$

$$
\begin{array}{r}
7 \\
\hline
\end{array}
$$

b. 24

$$
\begin{array}{r}
\times \quad 9 \\
\hline
\end{array}
$$

d. $\quad 47$

$$
\begin{array}{r} 
\\
\times \\
\hline
\end{array}
$$

$$
\begin{array}{r} 
\\
\times \quad 5 \\
\hline
\end{array}
$$

e. 29

$$
\begin{array}{r}
8 \\
\hline
\end{array}
$$

